

## Key

1. 100
2. 1,076
3. 8
4. 108
5.  $18\sqrt{14}$
6. 9
7. 64.95
8. 2,310

There are  $15C6 = 5,005$  ways to get from the origin to  $(9,6)$ . Some of these paths pass through  $(4,3)$  and others pass through  $(5,5)$ , and some pass through both. We subtract the ways which pass through  $(5,5)$  and the ways that pass through  $(4,3)$  then add back the ways that pass through both to avoid subtracting them twice. There are  $(7C3)(8C3) = 35 \times 56 = 1,960$  paths which pass through  $(4,3)$  and there are  $(10C5)(5C1) = 252 \times 5 = 1,260$  ways to get there through  $(5,5)$  but there are  $(7C3)(3C1)(5C1) = 35 \times 3 \times 5 = 525$  ways which pass through both points.  $5,005 - 1,960 - 1,260 + 525 = 2,310$  ways to get there.

9.  $25\sqrt{15}$
10.  $(53, 29, 6)$